Day 1: Angles

## Geometry: Angles

## Vocabulary



Acute angle: $0<\theta<90$ (between zero and 90 degrees)

Obtuse angle: $90<\theta<180$ (between 90 and 180 degrees)

Complementary angles: 90 degrees
Supplementary angles: 180 degrees

Angles on a line:


Angles at a point:


Opposite angles:


Congruent angles: equal size angles

How to name an angle:


## Proof $x=z$

$$
\left(\begin{array}{l}
\angle x+\angle y=180^{\circ} \\
\angle z+\angle y=180^{\circ} \\
\angle z=180^{\circ} \angle y
\end{array}\right.
$$

$$
y<x=180-\angle y
$$

$$
\begin{equation*}
\therefore \angle z=\angle x \tag{QED}
\end{equation*}
$$

"quod drat demonstrandum". It literally translates as "which was to be demonstrated"

$$
\begin{aligned}
& \angle x y z \\
& L z y x
\end{aligned}
$$

What is an angle that is adjacent to $\angle 5$ ?

$\angle 4$ or 16

Which angle is complementary to $\angle E F A$ ?


$\angle 4$ or 16


Which angle is supplementary to $\angle A E B$ ?


Which angles are congruent to $\angle 1$ ? Select all that apply.


## Find $x$



$$
x=117^{\circ}
$$



$$
x=110^{\circ}
$$



$$
\begin{aligned}
& x=108^{\circ} \\
& y=108^{\circ} \\
& z=72^{\circ}
\end{aligned}
$$



$$
\begin{aligned}
& a=55^{\circ} \\
& b=55^{\circ} \\
& c=70 \\
& d=110
\end{aligned}
$$

Challenge: Find $x$.


$$
\begin{aligned}
\frac{2 x+5}{3}+105 & =180 \\
x\left(\frac{2 x+5}{3}\right) & =(75) 3 \\
2 x+5 & =225 \\
2 x & =220 \\
x & =110
\end{aligned}
$$



$$
\begin{aligned}
3 x+15 & =75 \\
3 x & =60 \\
x & =20
\end{aligned}
$$

## Assign p(1) and (2) in Geom Booklet

Finding the interior angle sum of a polygon:


Find each angle if the polygon is regular.


